

Directional Gain and EIRP Calculations for Transmitters with Multiple Outputs

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Transmitters w/ Multiple Outputs (Same Band)

- Directional Gain of Multiple Antennas
- Relevance of Directional Gain to Compliance Tests
- Directional Gain Calculation
 - Correlation
 - Co-polarized Antenna Configurations
 - Cross- polarized Antenna Configurations
 - Hybrid Antenna Configurations
 - Combination of Co- polarized and Cross Polarized Antennas



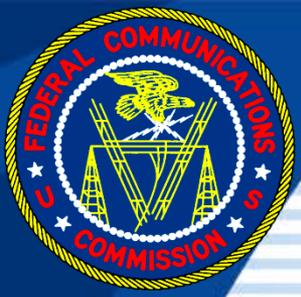
Directional Gain of Multiple Antennas

- Multiple antennas transmitting correlated Signals:
- Effective Directionality Greater than Directionality of Individual Antenna
- Directional Gain a Function of
 - Relative Phase of the Transmitted Signals
 - Relative Location of the Antennas
 - Number of Antennas
 - Excitation Method of Each Antenna
- This Increased Gain Is Referred to as Array Gain in FCC KDB Publications



Relevance of Directional Gain to Compliance Tests

- When Requirements Stated in Terms of Conducted Power Assuming Certain Antenna Gain
 - 15.247, 15.407, etc.
- When Radiated Power Is Verified Through (Conducted) Power Measurement
 - Antenna Gain Needed to Calculate EIRP



Directional Gain and EIRP Calculation

Co-polarized Antenna Configuration



Directional Gain Calculations (co-pol)

In-Band Measurement, Equal Antenna Gains

- If Any Transmit Signals Are Correlated:
 - Directional Gain= $G_{ant} + 10 \log(N_{ant}) \text{ dBi}$
 - N_{ant} : Number of Transmit Antennas
 - G_{ant} : Gain of Individual Antennas (Same for Each Antenna)
- If All Transmit Signals Are Completely Uncorrelated:
 - Directional Gain= G_{ant}



Directional Gain Calculations (co-pol)

In-Band Measurement, Unequal Antenna Gains

- If Any Transmit Signals Are Correlated:

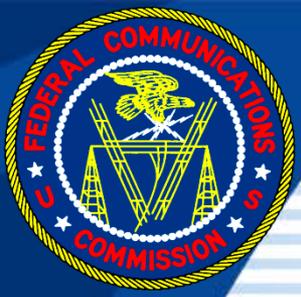
- Directional Gain= $10\log\left[\left(10^{\frac{G_1}{20}}+10^{\frac{G_2}{20}}+\dots+10^{\frac{G_n}{20}}\right)^2 / N_{ant}\right] \text{ dBi}$

- If All Transmit Signals Are Completely Uncorrelated:

- Directional Gain= $10\log\left[\left(10^{\frac{G_1}{10}}+10^{\frac{G_2}{10}}+\dots+10^{\frac{G_n}{10}}\right)/N_{ant}\right] \text{ dBi}$

N_{ant} : Number of Transmit Antennas

G_1, G_2, \dots, G_n : Gain of Individual Antennas

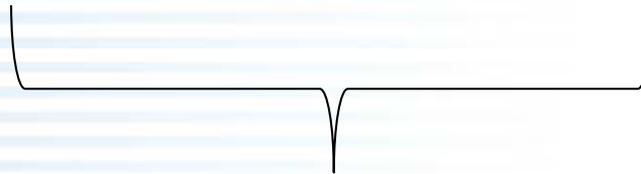


EIRP Calculations (co-pol)

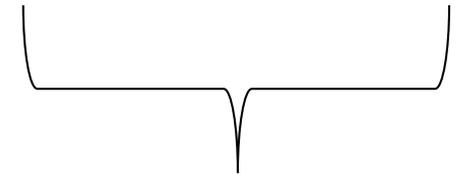
With Directional Gain Known

- EIRP (dB)= Total Transmit Power+ Directional Gain
- Example: N_{ant} Transmit Antennas Each with the same Gain Transmitting Correlated Signals

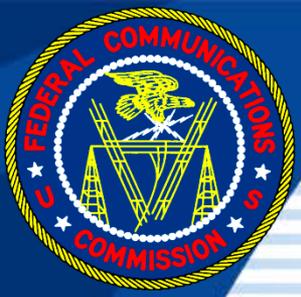
$$\text{EIRP} = (\text{Sum of Conducted Power}) + G_{ant} + 10 \log(N_{ant})$$



Total Transmit Power



Directional Gain



Directional Gain and EIRP Calculation

Cross-polarized (Orthogonal) Antenna Configuration



Directional Gain Calculations (cross pol)

Cross-polarized (Orthogonal) Antennas w/ $N_{ant}=2$:

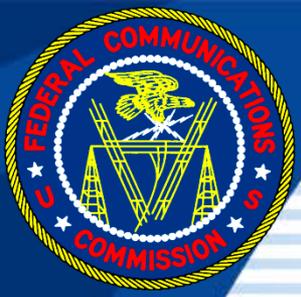
- Directional Gain = G_{ant}
- If Antenna Gains not the Same the Larger Gain Applies
- If $N_{ant} > 2$ and the Antennas are piecewise Orthogonal:
 - Directional Gain Is Calculated for every two Orthogonal Antennas and the Total Gain Is Calculated Either Algebraically or Vectorially



EIRP Calculations (cross pol)

Cross-polarized (Orthogonal) Antennas w/ $N_{ant}=2$:

- If Signals Completely Uncorrelated, or One Output is a 90 deg Phase-shifted Replica of the Other:
 - No Need to Sum the EIRPs
 - Each EIRP Must Be Below the Limit
- If Signals Correlated and No Phase Difference:
 - The Sum of the Two EIRPs Must Be Below the Limit



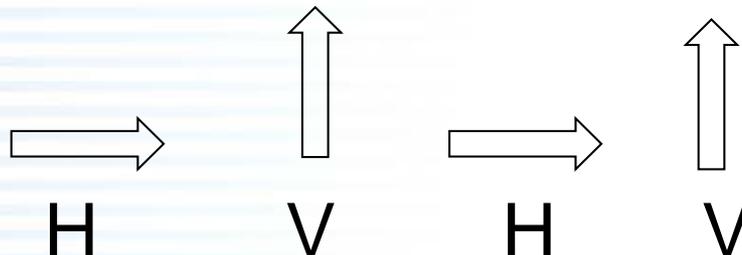
Directional Gain and EIRP Calculation

Hybrid Antenna Configuration



Hybrid Antenna Configuration

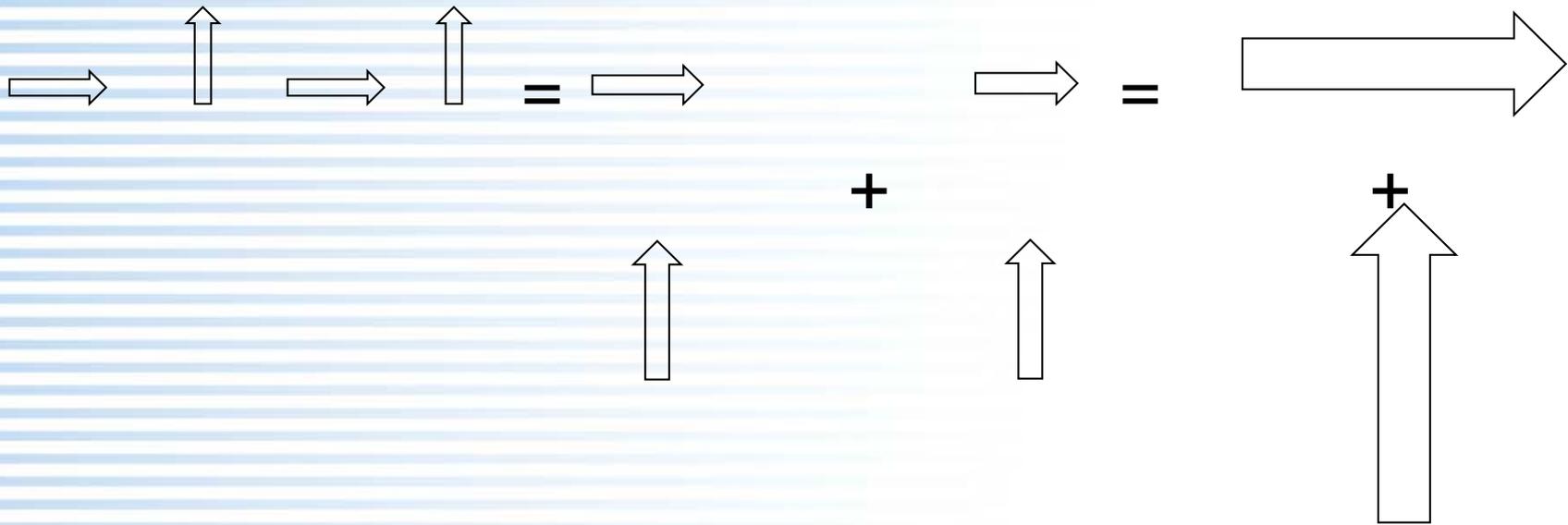
- A System that Utilizes a Combination of Co-polarized Radiators as well as Cross-polarized Radiators, for example:
- A Composite Transmitter with 4 Output Ports with 2 Vertically-Polarized Antennas and 2 Horizontally-polarized Antennas





Directional Gain and EIRP Calculation (Hybrid)

- Step 1: Break Down the System to Two Co-polarized Antennas
- Step 2: Compute the Gain for Co-polarized subgroup Individually
- Step 3: Apply the Cross-Polarized Guidance to Calculate the EIRP





References

- KDB Publications 662911 D01
- KDB Publications 662911 D02
- OET Report FCC/OET 13TR1003